Neural Networks 2

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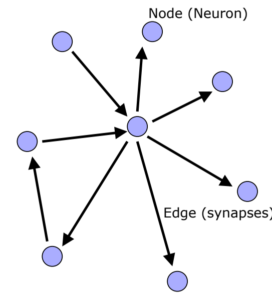
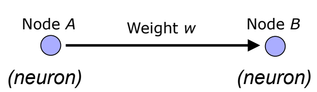
CS30
Spring 2015

Artificial Neural Networks





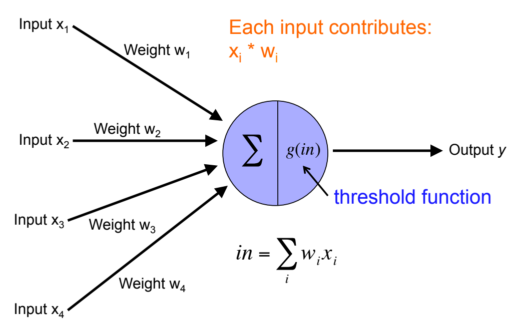
W is the strength of signal sent between A and B.

If *A* fires and *w* is **positive**, then *A* **stimulates** *B*.

If *A fires* and *w* is **negative**, then *A* **inhibits** *B*.

A Single Neuron/Perceptron

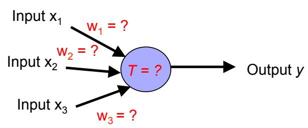
Each input contributes: $x_i * w_i$



$$in = \sum_i w_i x_i$$

Training neural networks

x_1	x_2	x_3	x_1 **and** x_2
0	0	0	1
0	1	0	0
1	0	0	1
1	1	0	0
0	0	1	1
0	1	1	1
1	0	1	1
1	1	1	0



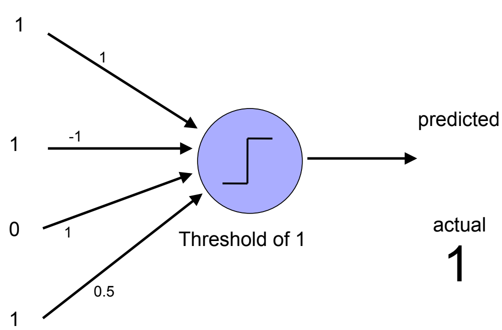
1. start with some initial weights and thresholds
2. show examples repeatedly to NN
3. update weights/thresholds by comparing NN output to actual output

Perceptron learning algorithm

repeat until you get all examples right:

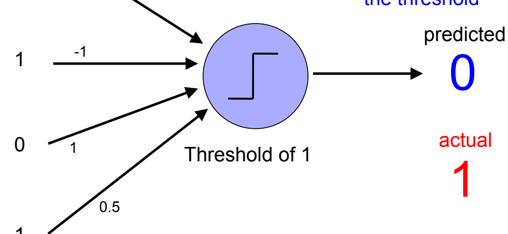
- for each "training" example:
  - calculate current prediction on example
  - if *wrong*:
    - update weights and threshold towards getting this example correct

Perceptron learning



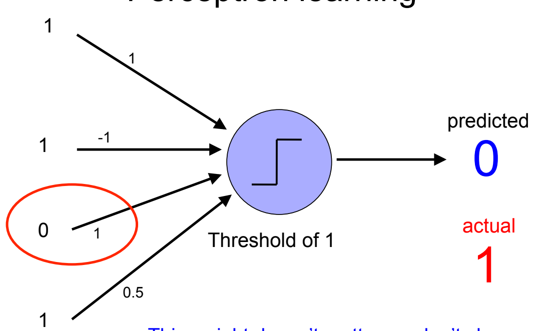
Perceptron learning

Weighted sum is 0.5, which is not equal or larger than the threshold



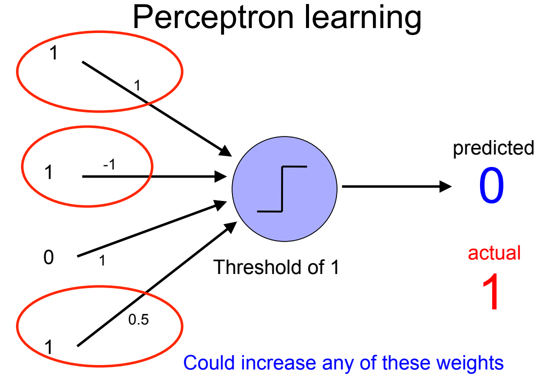
What could we adjust to make it right?

Perceptron learning



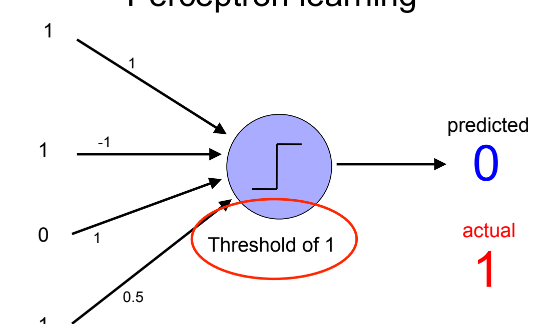
This weight doesn't matter, so don't change

Perceptron learning



Could increase any of these weights

Perceptron learning



Could decrease the threshold

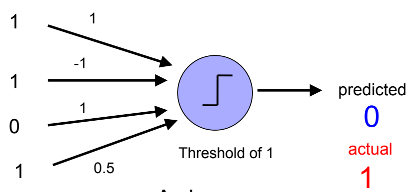
Perceptron update rule

- if *wrong*:
  - update weights and threshold towards getting this example correct
- if *wrong*:

$$w_i = w_i + \Delta w_i$$

$$\Delta w_i = \lambda * (\text{actual} - \text{predicted}) * x_i$$

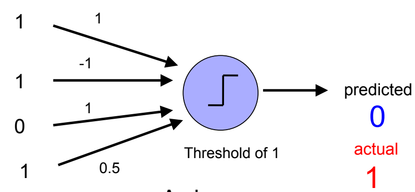
Perceptron learning



$w_i = w_i + \Delta wi$

$$\Delta w_i = \lambda * \underbrace{(\text{actual - predicted})}_{\text{What does this do in this case?}} * x_i$$

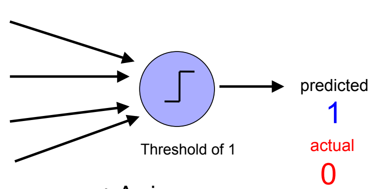
Perceptron learning



$w_i = w_i + \Delta wi$

$$\Delta w_i = \lambda * \underbrace{(\text{actual - predicted})}_{\text{causes us to increase the weights!}} * x_i$$

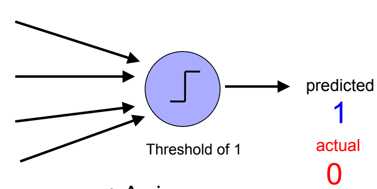
Perceptron learning



$w_i = w_i + \Delta wi$

$$\Delta w_i = \lambda * \underbrace{(\text{actual - predicted})}_{\text{What if predicted = 1 and actual = 0?}} * x_i$$

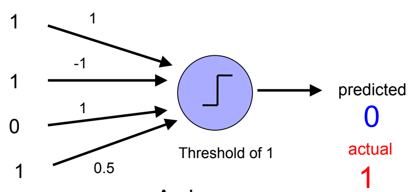
Perceptron learning



$w_i = w_i + \Delta wi$

$$\Delta w_i = \lambda * \underbrace{(\text{actual - predicted})}_{\begin{array}{l}\text{We're over the threshold, so want to decrease weights:} \\ \text{actual - predicted = -1}\end{array}} * x_i$$

Perceptron learning

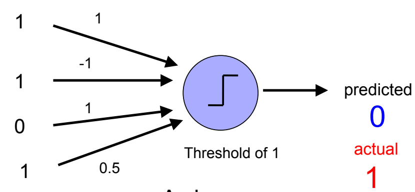


$w_i = w_i + \Delta wi$

$\Delta w_i = \lambda * (\text{actual - predicted}) * x_i$

What does this do?

Perceptron learning

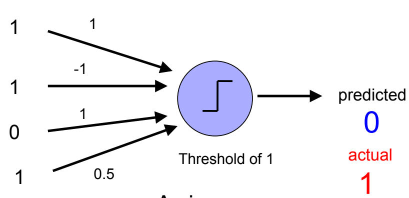


$w_i = w_i + \Delta wi$

$\Delta w_i = \lambda * (\text{actual - predicted}) * x_i$

Only adjust those weights that actually contributed!

Perceptron learning

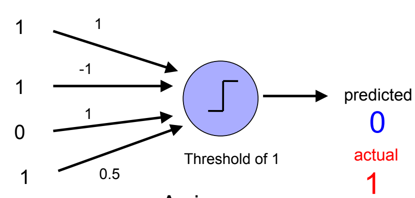


$w_i = w_i + \Delta wi$

$\Delta w_i = \lambda * (\text{actual - predicted}) * x_i$

What does this do?

Perceptron learning

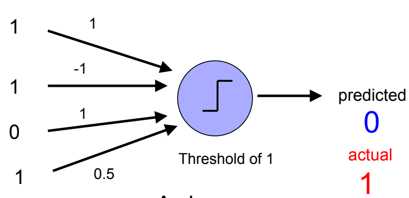


$w_i = w_i + \Delta wi$

$\Delta w_i = \lambda * (\text{actual - predicted}) * x_i$

"learning rate": value between 0 and 1 (e.g 0.1) adjusts how abrupt the changes are to the model

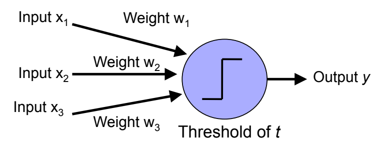
Perceptron learning



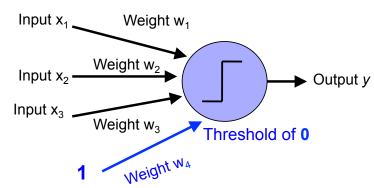
$w_i = w_i + \Delta wi$

$\Delta w_i = \lambda * (\text{actual - predicted}) * x_i$

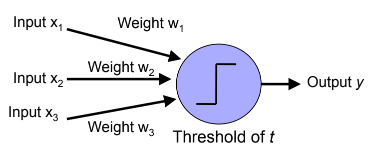
What about the threshold?



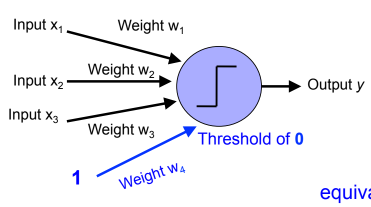
$$1 \text{ if } \sum_{i=1}^{3} w_i x_i \geq t$$



$$1 \text{ if } w_4 + \sum_{i=1}^{3} w_i x_i \geq 0$$



$$1 \text{ if } \sum_{i=1}^{3} w_i x_i \geq t$$



$$1 \text{ if } w_4 + \sum_{i=1}^{3} w_i x_i \geq 0$$

equivalent when $w_4 = -t$

Perceptron learning algorithm

initialize weights of the model randomly

repeat until you get all examples right:

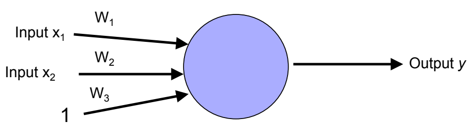
- for each "training" example (*in a random order*):
  - calculate current prediction on the example
  - if *wrong*:

    $w_i = w_i + \lambda * (\text{actual - predicted}) * x_i$

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

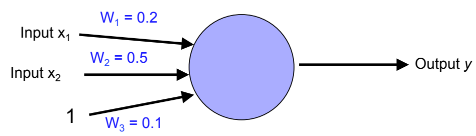
$\lambda = 0.1$

initialize with random weights



x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$\lambda = 0.1$

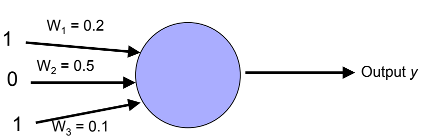


x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$\lambda = 0.1$

if wrong:

$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$



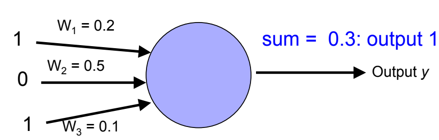
Right or wrong?

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$\lambda = 0.1$

if wrong:

$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$



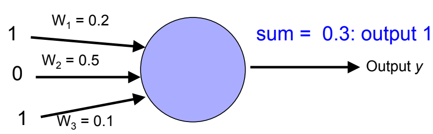
Wrong

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$\lambda = 0.1$

if wrong:

$w_i = w_i + \lambda * (\text{actual - predicted}) * x_i$



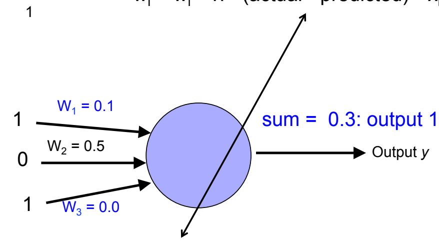
new weights?

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$\lambda = 0.1$

if wrong:

$w_i = w_i + \lambda * (\text{actual - predicted}) * x_i$



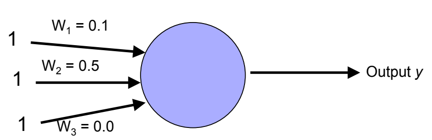
decrease (0-1=-1) all non-zero x_i by 0.1

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$\lambda = 0.1$

if wrong:

$w_i = w_i + \lambda * (\text{actual - predicted}) * x_i$



Right or wrong?

x_1	x_2	x_1 and x_2
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0	1	0
1	0	0
1	1	1

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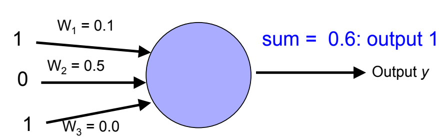
if wrong:

$w_i = w_i + \lambda * (\text{actual - predicted}) * x_i$



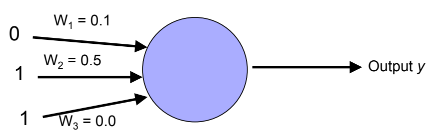
Right. No update!

x_1	x_2	x_1 **and** x_2
0	0	0
0	1	0
1	0	0
1	1	1

$\lambda = 0.1$

if wrong:

$w_i = w_i + \lambda * (\text{actual - predicted}) * x_i$



Right or wrong?

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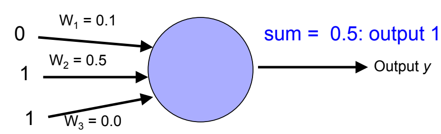

Wrong

x_1	x_2	x_1 **and** x_2
0	0	0
0	1	0
1	0	0
1	1	1

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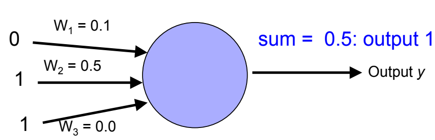
if wrong:

$w_i = w_i + \lambda * (\text{actual - predicted}) * x_i$



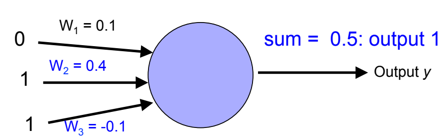
new weights?

x_1	x_2	x_1 **and** x_2
0	0	0
0	1	0
1	0	0
1	1	1

$\lambda = 0.1$

if wrong:

$w_i = w_i + \lambda * (\text{actual - predicted}) * x_i$



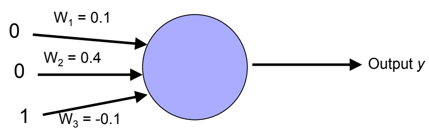
decrease (0-1=-1) all non-zero x_i by 0.1

x_1	x_2	x_1 **and** x_2
0	0	0
0	1	0
1	0	0
1	1	1

$\lambda = 0.1$

if wrong:

$w_i = w_i + \lambda * (\text{actual - predicted}) * x_i$



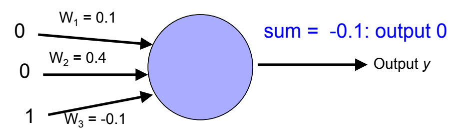
Right or wrong?

x_1	x_2	x_1 **and** x_2
0	0	0
0	1	0
1	0	0
1	1	1

$\lambda = 0.1$

if wrong:

$w_i = w_i + \lambda * (\text{actual - predicted}) * x_i$



Right. No update!

x_1	x_2	x_1 **and** x_2
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0	1	0
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1	1	1

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if wrong:

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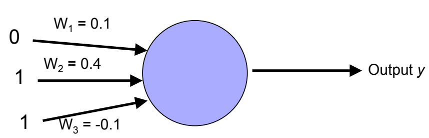

Right or wrong?

x_1	x_2	x_1 **and** x_2
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0	1	0
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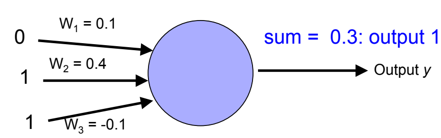
$\lambda = 0.1$

if wrong:

$w_i = w_i + \lambda * (\text{actual - predicted}) * x_i$



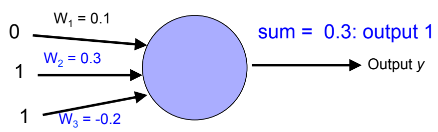
Wrong

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$\lambda = 0.1$

if wrong:

$w_i = w_i + \lambda * (\text{actual - predicted}) * x_i$



decrease (0-1=-1) all non-zero x_i by 0.1

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$\lambda = 0.1$

if wrong:

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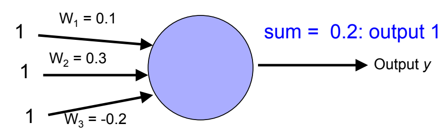

Right. No update!

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
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1	1	1

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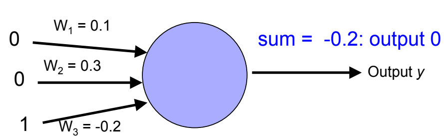

Right. No update!

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$\lambda = 0.1$

if wrong:

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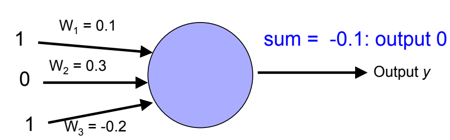

Right. No update!

x_1	x_2	x_1 **and** x_2
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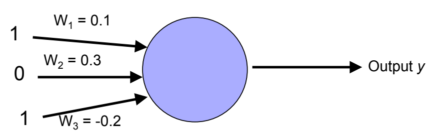
0	1	0
1	0	0
1	1	1

$\lambda = 0.1$

if wrong:

$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$



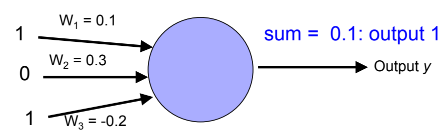
Are they all right?

x_1	x_2	x_1 **and** x_2
0	0	0
0	1	0
1	0	0
1	1	1

$\lambda = 0.1$

if wrong:

$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$



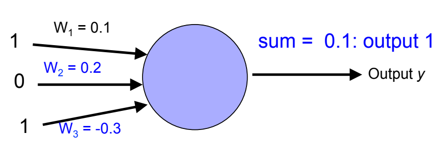
Wrong

x_1	x_2	x_1 **and** x_2
0	0	0
0	1	0
1	0	0
1	1	1

$\lambda = 0.1$

if wrong:

$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$



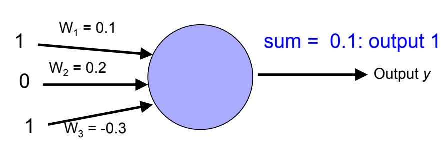
decrease (0-1=-1) all non-zero x_i by 0.1

x_1	x_2	x_1 **and** x_2
0	0	0
0	1	0
1	0	0
1	1	1

$\lambda = 0.1$

if wrong:

$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$



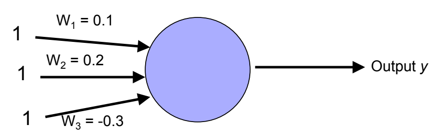
Are they all right?

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$\lambda = 0.1$

if wrong:

$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$



We've learned AND!

Learning in multilayer networks

Similar idea as perceptrons

Examples are presented to the network

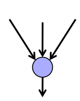
If the network computes an output that matches the desired, nothing is done

If there is an error, then the weights are adjusted to balance the error

Learning in multilayer networks

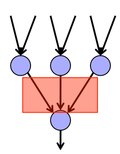
Key idea for perceptron learning: if the perceptron's output is different than the expected output, update the weights

Challenge: for multilayer networks, we don't know what the expected output/error is for the internal nodes



perceptron

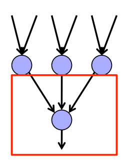
expected output?



multi-layer network

Backpropagation

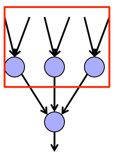
Say we get it wrong, and we now want to update the weights



We can update this layer just as if it were a perceptron

Backpropagation

Say we get it wrong, and we now want to update the weights



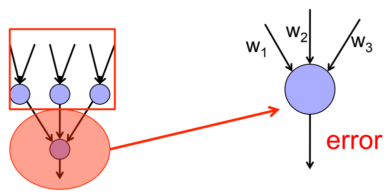
"back-propagate" the error:

Assume all of these nodes were responsible for some of the error

How can we figure out how much they were responsible for?

Backpropagation

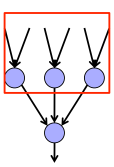
Say we get it wrong, and we now want to update the weights



error for node *i* is: w_i error

Backpropagation

Say we get it wrong, and we now want to update the weights



Update these weights and continue the process back through the network

Backpropagation

calculate the error at the output layer

backpropagate the error up the network

Update the weights based on these errors

Can be shown that this is the appropriate thing to do based on our assumptions

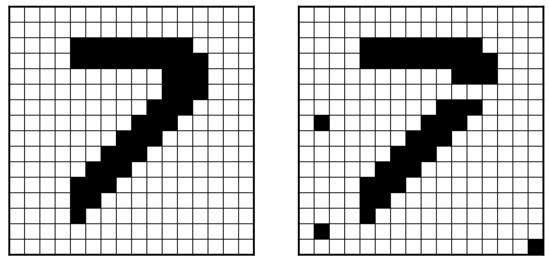
That said, many neuroscientists don't think the brain does backpropagation of errors

Neural network regression

Given enough hidden nodes, you can learn *any* function with a neural network

Challenges:

- overfitting – learning only the training data and not learning to generalize
- picking a network structure
- can require a lot of tweaking of parameters, preprocessing, etc.



Popular for digit recognition and many computer vision tasks

http://yann.lecun.com/exdb/mnist/

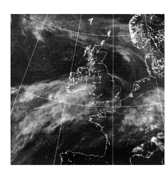
Cog sci people like NNs

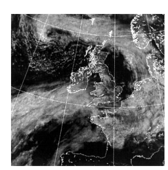
Expression/emotion recognition

- Gary Cottrell et al

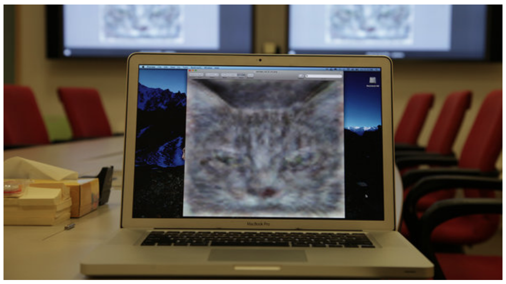
Language learning

Interpreting Satellite Imagery for Automated Weather Forecasting





What NNs learned from youtube



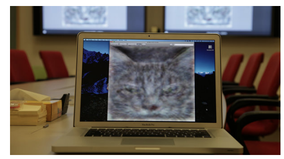
http://www.nytimes.com/2012/06/26/technology/in-a-big-network-of-computers-evidence-of-machine-learning.html

What NNs learned from youtube

trained on 10M snapshots from youtube videos

NN with 1 billion connections

16,000 processors



Summary

Perceptrons, one layer networks, are insufficiently expressive

Multi-layer networks are sufficiently expressive and can be trained by error back-propogation

Many applications including speech, driving, hand written character recognition, fraud detection, driving, etc.

Our python NN module

Data:

x_1	x_2	x_3	x_1 **and** x_2
0	0	0	1
0	1	0	0
1	0	0	1
1	1	0	0
0	0	1	1
0	1	1	1
1	0	1	1
1	1	1	0

```
table = \
[ ([0.0, 0.0, 0.0], [1.0]),
  ([0.0, 1.0, 0.0], [0.0]),
  ([1.0, 0.0, 0.0], [1.0]),
  ([1.0, 1.0, 0.0], [0.0]),
  ([0.0, 0.0, 1.0], [1.0]),
  ([0.0, 1.0, 1.0], [1.0]),
  ([1.0, 0.0, 1.0], [1.0]),
  ([1.0, 1.0, 1.0], [0.0]) ]
```

Data format

list of examples

```
table = \
[ ([0.0, 0.0, 0.0], [1.0]),
  ([0.0, 1.0, 0.0], [0.0]),
  ([1.0, 0.0, 0.0], [1.0]),
  ([1.0, 1.0, 0.0], [0.0]),
  ([0.0, 0.0, 1.0], [1.0]),
  ([0.0, 1.0, 1.0], [1.0]),
  ([1.0, 0.0, 1.0], [1.0]),
  ([1.0, 1.0, 1.0], [0.0]) ]
```

([0.0, 0.0, 0.0], [1.0])

input list output list

example = tuple

Training on the data

Construct a new network:

\>>> nn = neuralNet(3, 2, 1)

constructor: constructs a new NN object

input nodes

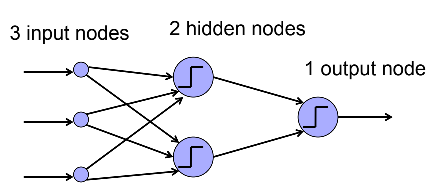
hidden nodes

output nodes

Training on the data

Construct a new network:

\>>> nn = neuralNet(3, 2, 1)



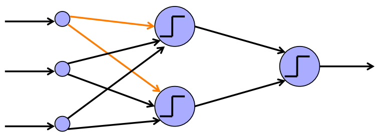
Training on the data

```
>>> nn.train(table)
error 0.195200
error 0.062292
error 0.031077
error 0.019437
error 0.013728
error 0.010437
error 0.008332
error 0.006885
error 0.005837
error 0.005047
```

by default trains 1000 iteration and prints out error values every 100 iterations

After training, can look at the weights

```
>>> nn.train(table)
>>> nn.getIHWeights()
[[-3.3435628797862624, -0.272324373735495],
 [-4.846203738642956, -4.601230952566068],
 [3.4233831101145973, 0.573534695637572],
 [2.9388429644152128, 1.8509761272713543]]
```



After training, can look at the weights

```
>>> nn.train(table)
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[[-3.3435628797862624, -0.272324373735495],
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```
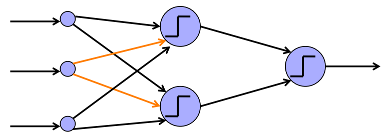
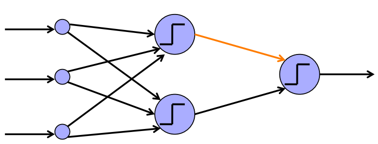



After training, can look at the weights

```
>>> nn.getHOWeights()
[[8.116192424400454],
 [5.358094903107918],
 [-4.373829543609533]]
```



Many parameters to play with

`nn.train(trainingData)` carries out a training cycle. As specified earlier, the training data is a list of input-output pairs. There are four optional arguments to the `train` function:

`learningRate` defaults to 0.5.

`momentumFactor` defaults to 0.1. The idea of momentum is discussed in the next section. Set it to 0 to suppress the affect of the momentum in the calculation.

`iterations` defaults to 1000. It specifies the number of passes over the training data.

`printInterval` defaults to 100. The value of the error is displayed after `printInterval` passes over the data; we hope to see the value decreasing. Set the value to 0 if you do not want to see the error values.

You may specify some, or all, of the optional arguments by name in the following format.

```
nn.train(trainingData,
         learningRate=0.8,
         momentumFactor=0.0,
         iterations=100,
         printInterval=5)
```

Calling with optional parameters

```
>>> nn.train(table, iterations = 5, printInterval = 1)
error 0.005033
error 0.005026
error 0.005019
error 0.005012
error 0.005005
```

Train vs. test

TrainData

input	output
0.0	0.00
0.2	0.04
0.4	0.16
0.6	0.36
0.8	0.64
1.0	1.00

TestData

input	output
0.3	0.09
0.5	0.25
0.7	0.49
0.8	0.64
0.9	0.81

```
>>> nn.train(trainData)
>>> nn.test(testData)
```

http://www.sciencebytes.org/2011/05/03/blueprint-for-the-brain/