

CFGS – TAKE 2

David Kauchak  
CS30 – Spring 2015

### Admin

Today's mentor hours moved to 6-8pm

Assignment 4 graded

Assignment 5

- how's it going?
- part A due tonight at 11:59pm
- part B due Friday at 6pm

### Course feedback

Thanks!

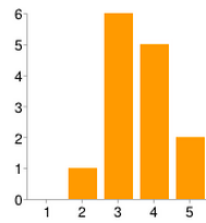
### Course feedback

Overall, how is the class going?

Score	Count
1	0
2	0
3	1
4	7
5	6

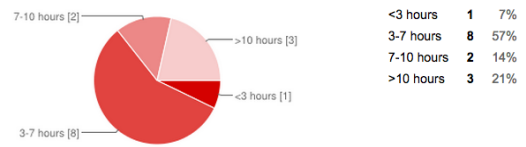
## Course feedback

How is the difficulty of the class?



## Course feedback

About how many hours a week do you spend on this class?



## Favorite thing about the course

Learning Python. It's pretty dope.

## Things to be improved

Sometimes a lot of the lecture material is covered too quickly. I would appreciate a slightly more comprehensive pace, and easier first examples.

Maybe focusing more time on reviewing the concepts that we have already learned just to make sure that the idea is really solidified it so that we can use it in a program.

Honestly, it's a little slow. But I don't really know how to improve that given that I know literally nothing about coding and need to be walked through things.

### Things to be improved

Also I would really enjoy more mentor sessions, on Monday, for example. Or even on Friday.

It would be helpful to have a tutor/ mentor session on Sunday nights so that if we run into questions/ issues on homework over the weekend, there is somewhere to get help before Tuesday, aka halfway through the week.

### Things to be improved

I was talking to a friend about how it'd be really nice to have a buddy to share how I code a function. I thought by watching another person code in a way that is different/similar to yours, you can understand the logic/style better and faster.

### Things to be improved

We haven't done that many assignments, but one of them had some grading I didn't understand. I feel like that was an anomaly though.

### Things to be improved

More high-five breaks!



## Other thoughts

I would really like to do Turing Machines in this class I think they're fun & have interesting connections/ applications to computation/ the human mind

## Comments in the future...

## Grammars

### Language view:

A grammar is a set of structural rules that govern the composition of sentences, phrases and words.

### Computational view:

A grammar (often called a "formal grammar") is a set of rules that describe what strings are valid in a formal language.

## CFG production rules

$$S \rightarrow NP VP$$

left hand side      right hand side  
(single symbol)      (one or more symbols)

### CFG example

Grammars "generate" or "derive" strings:

$S \rightarrow A B C$   
 $A \rightarrow I$   
 $B \rightarrow \text{really}$   
 $B \rightarrow \text{really}, B$   
 $C \rightarrow \text{like cs}$

S

### CFG example

Grammars "generate" or "derive" strings:

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We can apply a rule by substituting the symbol on the left hand side with the symbols on the right

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I really like cs

We can apply a rule by substituting the symbol on the left hand side with the symbols on the right

No more rules apply, so we're done!

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A really, really, B C

We can apply a rule by substituting the symbol on the left hand side with the symbols on the right

## CFG example

Grammars describe a language, i.e. the strings (aka sentences) that are part of that language

$S \rightarrow A B C$   
 $A \rightarrow I$   
 $B \rightarrow \text{really}$   
 $B \rightarrow \text{really, B}$   
 $C \rightarrow \text{like cs}$

I really, really, ... like cs

## What language does this represent?

$S \rightarrow aS$   
 $S \rightarrow E$   
 $E \rightarrow bE$   
 $E \rightarrow b$

## What language does this represent?

$S \rightarrow aS$   
 $S \rightarrow E$   
 $E \rightarrow bE$   
 $E \rightarrow b$

Two options      S



What language does this represent?

$S \rightarrow aS$   
 $S \rightarrow E$   
 $E \rightarrow bE$   
 $E \rightarrow b$

$S$   
 $\downarrow$   
 $aS$

What language does this represent?

$S \rightarrow aS$   
 $S \rightarrow E$   
 $E \rightarrow bE$   
 $E \rightarrow b$

$aS$   
 $\downarrow$   
 $aaS$

What language does this represent?

$S \rightarrow aS$   
 $S \rightarrow E$   
 $E \rightarrow bE$   
 $E \rightarrow b$

$aaS$   
 $\downarrow$   
 $aaaS$

- Can do this as many times as we want  
 - Keeps adding more a's to the front

What language does this represent?

$S \rightarrow aS$   
 $S \rightarrow E$   
 $E \rightarrow bE$   
 $E \rightarrow b$

$aaaS$   
 $\downarrow$   
 $aaaE$

Eventually, apply second rule

What language does this represent?

$S \rightarrow aS$   
 $S \rightarrow E$   
 $E \rightarrow bE$   
 $E \rightarrow b$

Two options

aaaE

What language does this represent?

$S \rightarrow aS$   
 $S \rightarrow E$   
 $E \rightarrow bE$   
 $E \rightarrow b$

aaaE  
↓  
aaabE

What language does this represent?

$S \rightarrow aS$   
 $S \rightarrow E$   
 $E \rightarrow bE$   
 $E \rightarrow b$

aaabE  
↓  
aaabbE

What language does this represent?

$S \rightarrow aS$   
 $S \rightarrow E$   
 $E \rightarrow bE$   
 $E \rightarrow b$

aaabbE  
↓  
aaabbbE

### What language does this represent?

$S \rightarrow aS$   
 $S \rightarrow E$   
 $E \rightarrow bE$   
 $E \rightarrow b$

$aaabbE$   
 $\downarrow$   
 $aaabb\dots bE$

- Can do this as many times as we want
- Keeps adding more b's to the end

### What language does this represent?

$S \rightarrow aS$   
 $S \rightarrow E$   
 $E \rightarrow bE$   
 $E \rightarrow b$

$aaabb\dots bE$   
 $\downarrow$   
 $aaabb\dots bb$

- Eventually, apply second rule

### What language does this represent?

$S \rightarrow aS$   
 $S \rightarrow E$   
 $E \rightarrow bE$   
 $E \rightarrow b$

$aaabb\dots bE$   
 $\downarrow$   
 $aaabb\dots bb$

Grammar represents all strings with zero or more a's followed by one or more b's

### Notational convenience

$S \rightarrow aS$   
 $S \rightarrow E$   
 $E \rightarrow bE$   
 $E \rightarrow b$



$S \rightarrow aS \mid E$   
 $E \rightarrow bE \mid b$

Often many ways to write the same language

$$S \rightarrow aS \mid E$$

$$E \rightarrow bE \mid b$$

$$S \rightarrow aS \mid E$$

$$E \rightarrow Eb \mid b$$

$$S \rightarrow aS \mid aaS \mid E$$

$$E \rightarrow Eb \mid b$$

What languages do these represent?

$$S \rightarrow aEa \mid bEb$$

$$E \rightarrow Ea \mid Eb \mid a \mid b$$

$$S \rightarrow aSb$$

$$S \rightarrow ab$$

$$S \rightarrow aaS \mid abS \mid baS \mid bbS \mid \epsilon$$

nothing

What languages do these represent?

$$S \rightarrow aEa \mid bEb$$

$$E \rightarrow Ea \mid Eb \mid a \mid b$$

all strings of a's and b's that start and end with the same letter

$$S \rightarrow aSb$$

$$S \rightarrow ab$$

strings of a's followed by an equal number of b's

$$S \rightarrow aaS \mid abS \mid baS \mid bbS \mid \epsilon$$

all strings of a's and b's with even length

Writing CFGs

Write a CFG to represent the language containing all strings that start with a.

$$S \rightarrow aT$$

$$T \rightarrow Ta \mid Tb \mid \epsilon$$

## Writing CFGs

Write a CFG to represent the language containing all strings with exactly two bs.

$$S \rightarrow TbTbT$$

$$T \rightarrow Ta \mid \epsilon$$

## CFG: Another example

Many possible CFGs for English, here is an example (fragment):

$$S \rightarrow NP VP$$

$$VP \rightarrow V NP$$

$$NP \rightarrow DetP N \mid DetP AdjP N$$

$$AdjP \rightarrow Adj \mid Adv AdjP$$

$$N \rightarrow \text{boy} \mid \text{girl}$$

$$V \rightarrow \text{sees} \mid \text{likes}$$

$$Adj \rightarrow \text{big} \mid \text{small}$$

$$Adv \rightarrow \text{very}$$

$$DetP \rightarrow a \mid \text{the}$$

## Derivations in a CFG

$$S \rightarrow NP VP$$

$$VP \rightarrow V NP$$

$$NP \rightarrow DetP N \mid DetP AdjP N$$

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$$Adv \rightarrow \text{very}$$

$$DetP \rightarrow a \mid \text{the}$$

S

What can we do?

## Derivations in a CFG

$$S \rightarrow NP VP$$

$$VP \rightarrow V NP$$

$$NP \rightarrow DetP N \mid DetP AdjP N$$

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$$Adv \rightarrow \text{very}$$

$$DetP \rightarrow a \mid \text{the}$$

S

## Derivations in a CFG

$S \rightarrow NP VP$   
 $VP \rightarrow V NP$   
 $NP \rightarrow DetP N \mid DetP AdjP N$   
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 $Adv \rightarrow very$   
 $DetP \rightarrow a \mid the$

NP VP

What can we do?

## Derivations in a CFG

$S \rightarrow NP VP$   
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NP VP

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DetP N VP

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$S \rightarrow NP VP$   
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DetP N VP

### Derivations in a CFG

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 $DetP \rightarrow a \mid the$

the boy VP

### Derivations in a CFG

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 $Adv \rightarrow very$   
 $DetP \rightarrow a \mid the$

the boy likes NP

### Derivations in a CFG

---

$S \rightarrow NP VP$   
 $VP \rightarrow V NP$   
 $NP \rightarrow DetP N \mid DetP AdjP N$   
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 $N \rightarrow boy \mid girl$   
 $V \rightarrow sees \mid likes$   
 $Adj \rightarrow big \mid small$   
 $Adv \rightarrow very$   
 $DetP \rightarrow a \mid the$

the boy likes a girl

### Derivations in a CFG: Order of Derivation Irrelevant

---

$S \rightarrow NP VP$   
 $VP \rightarrow V NP$   
 $NP \rightarrow DetP N \mid DetP AdjP N$   
 $AdjP \rightarrow Adj \mid Adv AdjP$   
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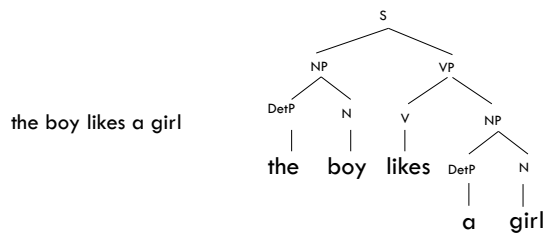
```

graph TD
    NPVP[NP VP] --> DetPNVP[DetP N VP]
    NPVP --> NPVNP[NP V NP]
    DetPNVP --> theboy[the boy]
    NPVNP --> likes[likes]
    NPVNP --> NPgirl[NP]
    NPgirl --> a[a]
    NPgirl --> girl[girl]
    
```

the boy likes a girl

## Derivations of CFGs

Derivation history shows a tree:



## Another CFG example

$S \rightarrow NP VP$

What can we generate?

$VP \rightarrow V \mid V ADV$

$NP \rightarrow ART PreNP$

$PreNP \rightarrow N \mid ADJ PreNP$

$ADV \rightarrow furiously \mid soothingly \mid intentionally$

$ADJ \rightarrow colorless \mid green \mid smelly$

$ART \rightarrow the \mid a$

$V \rightarrow sleeps \mid eats \mid swims \mid sprints$

$N \rightarrow idea \mid bagel \mid milk \mid cow$

## One last example

$S \rightarrow N$

$S \rightarrow ( S )$

$S \rightarrow S + S \mid S - S$

$S \rightarrow S * S \mid S / S$

$N \rightarrow 0 \mid 1 \mid 2 \mid \dots \mid 9$

$N \rightarrow NN$

What language does  
this CFG represent?

## One last example

$S \rightarrow N$

$S \rightarrow ( S )$

$S \rightarrow S + S \mid S - S$

$S \rightarrow S * S \mid S / S$

$N \rightarrow 0 \mid 1 \mid 2 \mid \dots \mid 9$

$N \rightarrow NN$

All arithmetic expressions!



### Parsing

---

Given a CFG and a sentence, determine the possible parse tree(s)

S -> NP VP  
 NP -> N  
 NP -> PRP  
 NP -> N PP  
 VP -> V NP  
 VP -> V NP PP  
 PP -> IN N  
 PRP -> I  
 V -> eat  
 N -> sushi  
 N -> tuna  
 IN -> with

I eat sushi with tuna

What parse trees are possible for this sentence?

How did you do it?

What if the grammar is much larger?

### Parsing

---

S -> NP VP  
 NP -> PRP  
 NP -> N PP  
 NP -> N  
 VP -> V NP  
 VP -> V NP PP  
 PP -> IN N  
 PRP -> I  
 V -> eat  
 N -> sushi  
 N -> tuna  
 IN -> with

What is the difference between these parses?

### CFGs implemented

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### Midterm

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Average: 26.3 (82.5%)

Median: 27.5 (86%)

Quartiles:

- Q1: 30 (97.5%)
- Q2: 27.5 (86%)
- Q3: 25 (78%)