

CS302 - Assignment 3

Due: Thursday, Feb. 21 at the beginning of class

Hand-in method: paper



<http://recursivelyrecursive.wordpress.com/category/recursive-humour/>

For this assignment you must use latex to generate your work.

1. (12 points) Give the asymptotic bounds for each of the recurrences below. Assume that $T(n)$ is constant for sufficiently small n . Make your bounds as tight as possible. If you use the master method, you must specify Θ bounds, but only need to specify O if you use another approach.

(a) $T(n) = 9T(n/3) + n^2$

- (b) $T(n) = 2T(n/2) + n^3$
- (c) $T(n) = 3T(n/2) + n \log n$
- (d) $T(n) = T(n - 2) + n$
- (e) $T(n) = 4T(n/2) + n^2 \sqrt{n}$
- (f) $T(n) = T(\sqrt{n}) + 1$

2. For the following problems, write **pseudocode** solutions and *state the worst case running time* (in terms of Θ or O where appropriate). You will be graded on the efficiency of your solutions.

- (a) (5 points) Given two lists of numbers A and B of lengths m and n respectively, return the intersection of the lists, i.e. all those numbers in A that also occur in B . You can use procedures that we've discussed in class, but no others (e.g. no hashtables). You can assume that in any given list, the numbers are unique.
- (b) (10 points) Given a *sorted* list of unique integers $A[1..n]$, determine if an entry exists such that $A[i] = i$. If an entry exists, return the index, otherwise, return *null*. (Hint: You can do better than $O(n)$. Think divide-and-conquer.)



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