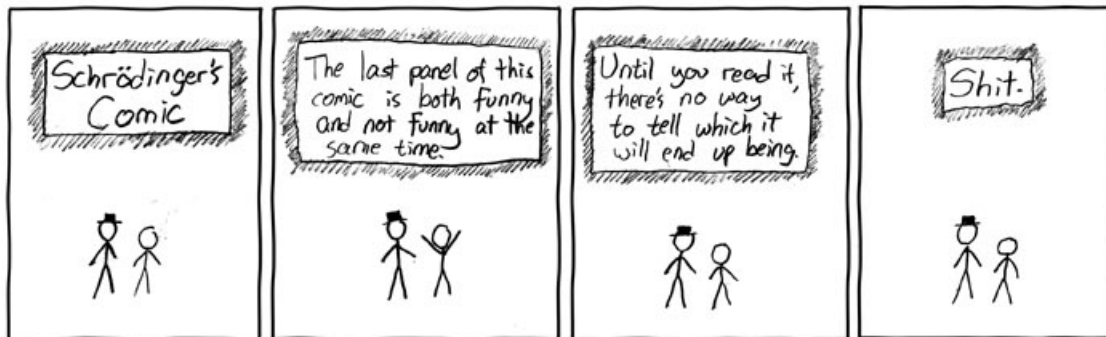


## CS302 - Assignment 21

Due: Thursday, May 9 at the beginning of class

Hand-in method: paper



<http://xkcd.com/45/>

For the problems below you may use any of the problems discussed in class or in the book as known NP-Complete problems.

1. [6 points] ZERO-SUM is the following problem: Given a set of integers  $S$  is there a subset that sum to 0?

Prove that ZERO-SUM is **NP-Hard**, i.e. you do not need to show that it is in NP, so you just need to provide a reduction function and show that it is correct.

2. [12 points] DOUBLE-SAT is the following problem: Given a boolean formula of  $n$  boolean variables  $x_1, x_2, \dots, x_n$  joined by  $m$  boolean connectives (one of:  $\wedge$  (AND),  $\vee$  (OR) and  $\neg$  (NOT)), are there **two** different assignments of the variables such that the boolean formula evaluates to 1 (i.e. true)? For example,  $(x_1 \vee \neg x_1 \vee \neg x_2) \wedge (x_2 \vee x_3) \wedge (\neg x_3)$  has two valid assignments,  $x_1 = 1, x_2 = 1, x_3 = 0$  and  $x_1 = 0, x_2 = 1, x_3 = 0$

Prove that DOUBLE-SAT is NP-Complete.